

Experience Rating Formula

Calculating the Mod

Calculating R assuming Poisson frequency

When to use a premium base for frequency

Poisson formula

Conclusions of paper

$$\frac{(\text{\# of claims with rating}) / (\text{on-level EP for rating at 'B' rates})}{(\text{\# of claims in total for class}) / (\text{class total on-level EP at 'B' rates})}$$

Mod = ZR + (1-Z)

Z = credibility

R = ratio of actual loss experience to expected loss experience

When to use a premium base for frequency

Calculating R assuming Poisson frequency

Hazam states that a premium base only eliminates maldistribution if:

- 1. High frequency territories are also high average premium territories.
- 2. Territorial (rate) differentials are proper.

| Years claim-free | R |
|------------------|---|
| 1+ | 0 |
| 0 | $\frac{1}{Pr(X \geq 1)} = \frac{1}{1 - e^{-\lambda}}$ |

where $\lambda = \frac{\text{\# of claims from class}}{\text{earned car years of insureds in class}}$

Conclusions of paper

Poisson formula

- 1. The experience of a single car for 1 year has significant and measurable credibility for experience rating.
- 2. Individual risk experience is more credible when there is more variance in loss experience within a risk class, which occurs in less refined risk classification systems.
- 3. The credibilities for varying years of experience should increase in proportion to the # of years of experience.

$$Pr(X = k) = \frac{\lambda^k e^{-\lambda}}{k!}$$

Credibility for 2 and 3 years of experience relative to 1 year

Bühlmann Credibility

Suppose X is a random variable with some distribution with parameter Θ , and Θ itself is a random variable with some distribution and additional parameters. In that case, the credibility of a sample of n observations from X is given by:

$$Z = \frac{n}{n+k}$$

n = # of claims in sample

$$k = \frac{E[Var(X|\Theta)]}{Var(E[X|\Theta])}$$

The credibility increases in proportion to the # of years only for low credibilities.

The closer the credibilities for 2 and 3 years of experience are to 2 and 3 times the 1 year credibility, then the less variation in insured's probability of an accident. This could be due to:

1. Less risks entering/exiting the portfolio.
2. Risk characteristics not changing much over time.